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**The parity of the number of irreducible factors for some pentanomials. (English summary)**

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The objective of the paper is to characterize the parity of the number of irreducible factors of some pentanomials over the binary field $\mathbb{F}_2$. More precisely, the authors cleverly use the classical theorem of Swan (first proved by Stickelberger), to prove several results of which the following is typical:

Let $m, n$ be positive numbers such that $m \equiv 2 \pmod 4$ and $n \equiv 1 \pmod 2$. Assume that $m \geq 2n + 2 + \delta$ where $\delta = 0$, $m$ is even and $\delta = 1$ otherwise. Then the pentanomial

$$x^m + x^{n+2} + x^{n+1} + x^n + 1$$

has an even number of prime (irreducible) factors over $\mathbb{F}_2$ if and only if $x = m, y = n$ or $x = -m, y = -n$ satisfies the condition

$$x \equiv 2 \pmod 8 \text{ and } y \in \{3, -1\} \pmod 8.$$

Reviewed by *Luis H. Gallardo*

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*Note: This list reflects references listed in the original paper as accurately as possible with no attempt to correct errors.*