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Duplication coefficients via generating functions. (English)

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The authors investigate a duplication type problem involving a polynomial set $\{P_n\}$ ($n \in \mathbb{N}$) for the relation $P_n = \sum_{m=0}^n C_m(n, a)P_m(x)$. A theorem of a general nature explicitly determines the associated coefficients for $C_m(n, a)$ for a Boas-Buck type generating relationship involving the polynomial set $\{P_n\}$ ($n \in \mathbb{N}$). Several interesting applications of the main result are depicted giving the closed-form expressions and recurrence relations satisfied by the duplication coefficients for the polynomials like, the Brenke polynomials, Brafman polynomials, Chaundy polynomials, Gould-Hopper polynomials, Shifted Jacobi polynomials, Charlier polynomials, Meixner polynomials and Krawtchouk polynomials.

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Classification :

***33C45** Orthogonal polynomials and functions of hypergeometric type

33C20 Generalized hypergeometric series

05A15 Combinatorial enumeration problems