

Comparison between **HypervanHoeij (Maxima) & FPS** **[rectohyperterm] (Maple)** **and** **LREtools[hypergeomsols] (Maple)**

Hypergeometric term solutions in Maple

The examples are taken from

https://www.math.fsu.edu/~hoeij/comparison_hypergeomsols

```

> restart
> read "vanHoeijREs.mpl"
> with(CodeTools):
> CPUtime(LREtools[hypergeomsols](RE[1]=0,v(n), {}, output=basis))
0.235,  $\left[ \left( -\frac{1}{a-1} \right)^n, \left( -\frac{1}{a-1} \right)^n n \right]$  (1)
> CPUtime(FPS[rectohyperterm](RE[1]=0,v(n), C))
0.141,  $\left\{ \left( -\frac{1}{a-1} \right)^n, \left( -\frac{1}{a-1} \right)^n n \right\}$  (2)
> CPUtime(LREtools[hypergeomsols](RE[2]=0,v(n), {}, output=basis))
0.078,  $\left[ \frac{\left( -\frac{1}{a} \right)^n \Gamma\left( n + \frac{1}{2} \right)}{\Gamma(n+1)} \right]$  (3)
> CPUtime(FPS[rectohyperterm](RE[2]=0,v(n), C))
0.141,  $\left\{ \frac{\left( -\frac{1}{a} \right)^n (2n)! 4^{-n}}{n!^2} \right\}$  (4)
> CPUtime(LREtools[hypergeomsols](RE[3]=0,v(n), {}, output=basis))

```

$$0., \left[\frac{\left(-\frac{1}{-3+a} \right)^n}{n} \right] \quad (5)$$

> CPUtime (FPS [rectohyperterm] (RE [3]=0, v(n), C))

$$0., \left\{ \frac{\left(-\frac{1}{-3+a} \right)^n}{n} \right\} \quad (6)$$

> CPUtime (LREtools [hypergeomsols] (RE [4]=0, v(n), {}, output=basis))

$$0.156, \left[\frac{\left(-\frac{1}{a} \right)^n \Gamma\left(n + \frac{1}{2} \right)}{\Gamma(n+1)} \right] \quad (7)$$

> CPUtime (FPS [rectohyperterm] (RE [4]=0, v(n), C))

$$0.078, \left\{ \frac{\left(-\frac{1}{a} \right)^n (2n)! 4^{-n}}{n!^2} \right\} \quad (8)$$

> CPUtime (LREtools [hypergeomsols] (RE [5]=0, v(n), {}, output=basis))

$$0., \left[\left(-\frac{1}{a} \right)^n, \left(-\frac{3}{3a-1} \right)^n, \left(-\frac{3}{3a-1} \right)^n n \right] \quad (9)$$

> CPUtime (FPS [rectohyperterm] (RE [5]=0, v(n), C))

$$0.063, \left\{ \left(-\frac{1}{a} \right)^n, \left(-\frac{3}{3a-1} \right)^n, \left(-\frac{3}{3a-1} \right)^n n \right\} \quad (10)$$

> CPUtime (LREtools [hypergeomsols] (RE [6]=0, v(n), {}, output=basis))

$$0.031, \left[\frac{\left(-\frac{1}{a} \right)^n (2a^2 - 2an + n^2 + 4a - 3n + 2)}{n(n-1)(n-2)}, \frac{\left(-\frac{1}{a+1} \right)^n}{n(n-1)(n-2)} \right] \quad (11)$$

> CPUtime (FPS [rectohyperterm] (RE [6]=0, v(n), C))

$$0.047, \left\{ \frac{\left(-\frac{1}{a+1} \right)^n}{n(n-1)(n-2)}, \frac{\left(-\frac{1}{a} \right)^n (2a^2 - 2an + n^2 + 4a - 3n + 2)}{n(n-1)(n-2)} \right\} \quad (12)$$

> CPUtime (LREtools [hypergeomsols] (RE [7]=0, v(n), {}, output=basis))

$$0.062, \left[\left(-\frac{1}{a} \right)^n (3a+n+1) \right] \quad (13)$$

> CPUtime (FPS [rectohyperterm] (RE [7]=0, v(n), C))

$$0.063, \left\{ \left(-\frac{1}{a} \right)^n (3a+n+1) \right\} \quad (14)$$

> CPUtime (LREtools [hypergeomsols] (RE [8]=0, v(n), {}, output=basis))

$$0.046, \left[\left(-\frac{1}{a+1} \right)^n \right] \quad (15)$$

> CPUtime (FPS [rectohyperterm] (RE [8]=0, v(n), C))

$$0.032, \left\{ \left(-\frac{1}{a+1} \right)^n \right\} \quad (16)$$

> CPUtime (LREtools [hypergeomsols] (RE [9]=0, v(n), {}, output=basis))

(17)

$$0.109, 0 \quad (17)$$

> CPUtime (FPS [rectohyperterm] (RE [9]=0, v(n), C))

$$0.016, \emptyset \quad (18)$$

> CPUtime (LREtools [hypergeomsols] (RE [10]=0, v(n), {}, output=basis))

$$0.172, \left[\left(-\frac{1}{a} \right)^n (n+4)(n+3)(n+2)(n+1), \left(-\frac{1}{a-1} \right)^n (n+4)(n+3)(n+2)(n+1)(a-n-6) \right] \quad (19)$$

> CPUtime (FPS [rectohyperterm] (RE [10]=0, v(n), C))

$$0.031, \left\{ \left(-\frac{1}{a} \right)^n (n+4)(n+3)(n+2)(n+1), \left(-\frac{1}{a-1} \right)^n (n+4)(n+3)(n+2)(n+1)(a-n-6) \right\} \quad (20)$$

> CPUtime (LREtools [hypergeomsols] (RE [11]=0, v(n), {}, output=basis))

$$0., 0 \quad (21)$$

> CPUtime (FPS [rectohyperterm] (RE [11]=0, v(n), C))

$$0., \emptyset \quad (22)$$

> CPUtime (LREtools [hypergeomsols] (RE [12]=0, v(n), {}, output=basis))

$$0.157, \left[\frac{(-1)^n}{\Gamma(n+1)}, \frac{1^n}{\Gamma(n+1)} \right] \quad (23)$$

> CPUtime (FPS [rectohyperterm] (RE [12]=0, v(n), C))

$$0.156, \left\{ \frac{\text{RootOf}(Z^2+1)^n}{n!} \right\} \quad (24)$$

> CPUtime (LREtools [hypergeomsols] (RE [13]=0, v(n), {}, output=basis))

$$0.047, \left[\frac{\left(-\frac{1}{a} \right)^n (3a-n+3)}{n(n-1)(n-2)(n-3)}, \frac{\left(-\frac{3}{2+3a} \right)^n (3a+n-1)}{n(n-1)(n-2)(n-3)} \right] \quad (25)$$

> CPUtime (FPS [rectohyperterm] (RE [13]=0, v(n), C))

$$0.062, \left\{ \frac{\left(-\frac{3}{2+3a} \right)^n (3a+n-1)}{n(n-1)(n-2)(n-3)}, \frac{(n-3a-3) \left(-\frac{1}{a} \right)^n}{n(n-1)(n-2)(n-3)} \right\} \quad (26)$$

> CPUtime (LREtools [hypergeomsols] (RE [14]=0, v(n), {}, output=basis))

$$0.016, \left[\left(-\frac{1}{a-1} \right)^n \right] \quad (27)$$

> CPUtime (FPS [rectohyperterm] (RE [14]=0, v(n), C))

$$0.031, \left\{ \left(-\frac{1}{a-1} \right)^n \right\} \quad (28)$$

> CPUtime (LREtools [hypergeomsols] (RE [15]=0, v(n), {}, output=basis))

$$0.406, \left[\left(-\frac{1}{a+1} \right)^n, \left(-\frac{1}{a-1} \right)^n, \left(-\frac{1}{a+1} \right)^n, \left(-\frac{1}{a-1} \right)^n \right] \quad (29)$$

> CPUtime (FPS [rectohyperterm] (RE [15]=0, v(n), C))

$$(30)$$

$$0.250, \left\{ \left(-\frac{1}{a-1} \right)^n, \left(-\frac{1}{a+1} \right)^n, \text{RootOf}(1 + (a^2 + 1) _Z^2 + 2 _Z a)^n \right\} \quad (30)$$

$$\begin{aligned} &> \text{CPUtime}(\text{LREtools}[\text{hypergeomsols}] (\text{RE}[16]=0, \mathbf{v}(n), \{\}, \text{output}=\text{basis})) \\ &\quad 0.078, 0 \end{aligned} \quad (31)$$

$$\begin{aligned} &> \text{CPUtime}(\text{FPS}[\text{rectohyperterm}] (\text{RE}[16]=0, \mathbf{v}(n), \mathbf{C})) \\ &\quad 0.156, \emptyset \end{aligned} \quad (32)$$

$$\begin{aligned} &> \text{CPUtime}(\text{LREtools}[\text{hypergeomsols}] (\text{RE}[17]=0, \mathbf{v}(n), \{\}, \text{output}=\text{basis})) \\ &\quad 0.016, 0 \end{aligned} \quad (33)$$

$$\begin{aligned} &> \text{CPUtime}(\text{FPS}[\text{rectohyperterm}] (\text{RE}[17]=0, \mathbf{v}(n), \mathbf{C})) \\ &\quad 0.031, \emptyset \end{aligned} \quad (34)$$

$$\begin{aligned} &> \text{CPUtime}(\text{LREtools}[\text{hypergeomsols}] (\text{RE}[18]=0, \mathbf{v}(n), \{\}, \text{output}=\text{basis})) \\ &\quad 0.016, 0 \end{aligned} \quad (35)$$

$$\begin{aligned} &> \text{CPUtime}(\text{FPS}[\text{rectohyperterm}] (\text{RE}[18]=0, \mathbf{v}(n), \mathbf{C})) \\ &\quad 0.047, \emptyset \end{aligned} \quad (36)$$

$$\begin{aligned} &> \text{CPUtime}(\text{LREtools}[\text{hypergeomsols}] (\text{RE}[19]=0, \mathbf{v}(n), \{\}, \text{output}=\text{basis})) \\ &\quad 0.094, \left[\frac{\left(-\frac{1}{a} \right)^n}{n(n-1)}, \left(-\frac{1}{a} \right)^n \right] \end{aligned} \quad (37)$$

$$\begin{aligned} &> \text{CPUtime}(\text{FPS}[\text{rectohyperterm}] (\text{RE}[19]=0, \mathbf{v}(n), \mathbf{C})) \\ &\quad 0.093, \left\{ \left(-\frac{1}{a} \right)^n, \frac{\left(-\frac{1}{a} \right)^n}{n(n-1)} \right\} \end{aligned} \quad (38)$$

$$\begin{aligned} &> \text{CPUtime}(\text{LREtools}[\text{hypergeomsols}] (\text{RE}[20]=0, \mathbf{v}(n), \{\}, \text{output}=\text{basis})) \\ &\quad 0.078, \left[\frac{\left(-\frac{1}{a} \right)^n}{n(n-1)(n-2)(n-3)(n-4)} \right] \end{aligned} \quad (39)$$

$$\begin{aligned} &> \text{CPUtime}(\text{FPS}[\text{rectohyperterm}] (\text{RE}[20]=0, \mathbf{v}(n), \mathbf{C})) \\ &\quad 0.110, \left\{ \frac{\left(-\frac{1}{a} \right)^n}{n(n-1)(n-2)(n-3)(n-4)} \right\} \end{aligned} \quad (40)$$

$$\begin{aligned} &> \text{CPUtime}(\text{LREtools}[\text{hypergeomsols}] (\text{RE}[21]=0, \mathbf{v}(n), \{\}, \text{output}=\text{basis})) \\ &\quad 0.016, \left[\left(-\frac{1}{a} \right)^n, \left(-\frac{1}{a} \right)^n n, \left(-\frac{1}{a-1} \right)^n, \left(-\frac{2}{2a+1} \right)^n \right] \end{aligned} \quad (41)$$

$$\begin{aligned} &> \text{CPUtime}(\text{FPS}[\text{rectohyperterm}] (\text{RE}[21]=0, \mathbf{v}(n), \mathbf{C})) \\ &\quad 0.203, \left\{ \left(-\frac{1}{a} \right)^n, \left(-\frac{1}{a-1} \right)^n, \left(-\frac{2}{2a+1} \right)^n, \left(-\frac{1}{a} \right)^n n \right\} \end{aligned} \quad (42)$$

$$\begin{aligned} &> \text{CPUtime}(\text{LREtools}[\text{hypergeomsols}] (\text{RE}[22]=0, \mathbf{v}(n), \{\}, \text{output}=\text{basis})) \\ &\quad 0., 0 \end{aligned} \quad (43)$$

$$\begin{aligned} &> \text{CPUtime}(\text{FPS}[\text{rectohyperterm}] (\text{RE}[22]=0, \mathbf{v}(n), \mathbf{C})) \\ &\quad 0., \emptyset \end{aligned} \quad (44)$$

$$\begin{aligned} &> \text{CPUtime}(\text{LREtools}[\text{hypergeomsols}] (\text{RE}[23]=0, \mathbf{v}(n), \{\}, \text{output}=\text{basis})) \\ &\quad 0.063, \left[\frac{(-1)^n}{\Gamma(n+1)}, \frac{1^n}{\Gamma(n+1)} \right] \end{aligned} \quad (45)$$

> CPUtime (FPS [rectohyperterm] (RE [23]=0, v(n), C))

$$0.078, \left\{ \frac{\text{RootOf}(\underline{Z}^2 + 1)^n}{n!} \right\} \quad (46)$$

> CPUtime (LREtools [hypergeomsols] (RE [24]=0, v(n), {}, output=basis))

$$0.047, \left[\frac{(-1)^n}{\Gamma(n+1)}, \frac{1}{\Gamma(n+1)} \right] \quad (47)$$

> CPUtime (FPS [rectohyperterm] (RE [24]=0, v(n), C))

$$0.078, \left\{ \frac{1}{n!}, \frac{(-1)^n}{n!} \right\} \quad (48)$$

> CPUtime (LREtools [hypergeomsols] (RE [25]=0, v(n), {}, output=basis))

$$0.031, 0 \quad (49)$$

> CPUtime (FPS [rectohyperterm] (RE [25]=0, v(n), C))

$$0.016, \emptyset \quad (50)$$

> CPUtime (LREtools [hypergeomsols] (RE [26]=0, v(n), {}, output=basis))

$$0.156, \left[\frac{(-1)^n}{\Gamma(n+1)}, \frac{1}{\Gamma(n+1)}, \frac{n}{\Gamma(n+1)}, \frac{1^n}{\Gamma(n+1)}, \frac{(-1)^n}{\Gamma(n+1)}, \frac{\left(-\frac{1}{2} + \frac{I\sqrt{3}}{2}\right)^n}{\Gamma(n+1)}, \frac{\left(-\frac{1}{2} - \frac{I\sqrt{3}}{2}\right)^n}{\Gamma(n+1)} \right] \quad (51)$$

> CPUtime (FPS [rectohyperterm] (RE [26]=0, v(n), C))

$$0.219, \left\{ \frac{1}{n!}, \frac{n}{n!}, \frac{(-1)^n}{n!}, \frac{\text{RootOf}(\underline{Z}^2 + 1)^n}{n!}, \frac{\text{RootOf}(\underline{Z}^2 + \underline{Z} + 1)^n}{n!} \right\} \quad (52)$$

> CPUtime (LREtools [hypergeomsols] (RE [27]=0, v(n), {}, output=basis))

$$0.093, \left[\left(-\frac{1}{a-1}\right)^n, \left(-\frac{1}{a+1}\right)^n \right] \quad (53)$$

> CPUtime (FPS [rectohyperterm] (RE [27]=0, v(n), C))

$$0.141, \left\{ \left(-\frac{1}{a-1}\right)^n, \left(-\frac{1}{a+1}\right)^n \right\} \quad (54)$$

> CPUtime (LREtools [hypergeomsols] (RE [28]=0, v(n), {}, output=basis))

$$0.281, \left[\frac{(-1)^n}{\Gamma(n+1)}, \frac{1^n}{\Gamma(n+1)} \right] \quad (55)$$

> CPUtime (FPS [rectohyperterm] (RE [28]=0, v(n), C))

$$0.594, \left\{ \frac{\text{RootOf}(\underline{Z}^2 + 1)^n}{n!} \right\} \quad (56)$$

> CPUtime (LREtools [hypergeomsols] (RE [29]=0, v(n), {}, output=basis))

$$0.422, \left[\left(-\frac{1}{a-1}\right)^n, \left(-\frac{1}{a+1}\right)^n \right] \quad (57)$$

> CPUtime (FPS [rectohyperterm] (RE [29]=0, v(n), C))

$$0.531, \left\{ \left(-\frac{1}{a-1}\right)^n, \left(-\frac{1}{a+1}\right)^n \right\} \quad (58)$$

- > CPUtime (LREtools [hypergeomsols] (RE [30]=0, v(n), {}, output=basis))
0.515, $\left[\left(-\frac{1}{a-1}\right)^n, \left(-\frac{1}{a+1}\right)^n, \frac{(-1)^n}{\Gamma(n+1)}, \frac{\Gamma^n}{\Gamma(n+1)} \right]$ (59)
- > CPUtime (FPS [rectohyperterm] (RE [30]=0, v(n), C))
0.797, $\left\{ \left(-\frac{1}{a-1}\right)^n, \left(-\frac{1}{a+1}\right)^n, \frac{\text{RootOf}(Z^2+1)^n}{n!} \right\}$ (60)
- > CPUtime (LREtools [hypergeomsols] (RE [31]=0, v(n), {}, output=basis))
0.047, $\left[\frac{\Gamma^n}{\Gamma(n+1)}, \frac{(-1)^n}{\Gamma(n+1)} \right]$ (61)
- > CPUtime (FPS [rectohyperterm] (RE [31]=0, v(n), C))
0.031, $\left\{ \frac{\text{RootOf}(Z^2+1)^n}{n!} \right\}$ (62)
- > CPUtime (LREtools [hypergeomsols] (RE [32]=0, v(n), {}, output=basis))
0.047, 0 (63)
- > CPUtime (FPS [rectohyperterm] (RE [32]=0, v(n), C))
0.047, \emptyset (64)
- > CPUtime (LREtools [hypergeomsols] (RE [33]=0, v(n), {}, output=basis))
0.062, $\left[\left(-\frac{1}{a}\right)^n, \left(-\frac{1}{a-1}\right)^n \right]$ (65)
- > CPUtime (FPS [rectohyperterm] (RE [33]=0, v(n), C))
0.094, $\left\{ \left(-\frac{1}{a}\right)^n, \left(-\frac{1}{a-1}\right)^n \right\}$ (66)
- > CPUtime (LREtools [hypergeomsols] (RE [34]=0, v(n), {}, output=basis))
0.031, $\left[\left(-\frac{1}{a+2}\right)^n (n+1) \right]$ (67)
- > CPUtime (FPS [rectohyperterm] (RE [34]=0, v(n), C))
0.047, $\left\{ \left(-\frac{1}{a+2}\right)^n (n+1) \right\}$ (68)
- > CPUtime (LREtools [hypergeomsols] (RE [35]=0, v(n), {}, output=basis))
0., 0 (69)
- > CPUtime (FPS [rectohyperterm] (RE [35]=0, v(n), C))
0.015, \emptyset (70)
- > CPUtime (LREtools [hypergeomsols] (RE [36]=0, v(n), {}, output=basis))
0.047, $\left[\left(-\frac{1}{a-1}\right)^n \right]$ (71)
- > CPUtime (FPS [rectohyperterm] (RE [36]=0, v(n), C))
0.047, $\left\{ \left(-\frac{1}{a-1}\right)^n \right\}$ (72)

HYPERGEOMETRIC TERM SOLUTIONS IN MAXIMA

(% i1) `batchload(vanHoeijsREs)$`

(% i2) `batchload(HyperTermHoloRE)$`

Hypergeometric terms and holonomic recurrence equations

Version 1.0

Execute 'Infos()' for details

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(% i3) `showtime:true$`

Evaluation took 0.0000 seconds (0.0000 elapsed) using 0 bytes.

(% i4) `HypervanHoeij(RE[1],v[n],C);`

Evaluation took 0.0000 seconds (0.0060 elapsed) using 1.375 MB.

$$\left\{ \left(-\frac{1}{a-1} \right)^n, \left(-\frac{1}{a-1} \right)^n n \right\} \quad (\% \text{ o4})$$

(% i5) `HypervanHoeij(RE[2],v[n],C);`

Evaluation took 0.0160 seconds (0.0170 elapsed) using 3.812 MB

$$\left\{ \frac{\left(-\frac{1}{a} \right)^n (2n)!}{4^n n!^2} \right\} \quad (\% \text{ o5})$$

(% i6) `HypervanHoeij(RE[3],v[n],C);`

Evaluation took 0.0150 seconds (0.0050 elapsed) using 832.000 KB

$$\left\{ \frac{\left(-\frac{1}{a-3} \right)^n}{n} \right\} \quad (\% \text{ o6})$$

(% i7) `HypervanHoeij(RE[4],v[n],C);`

Evaluation took 0.0310 seconds (0.0260 elapsed) using 8.685 MB

$$\left\{ \frac{\left(-\frac{1}{a} \right)^n (2n)!}{4^n n!^2} \right\} \quad (\% \text{ o7})$$

(% i8) HypervanHoeij(RE[5],v[n],C);

Evaluation took 0.0160 seconds (0.0220 elapsed) using 7.373 MB

$$\left\{ \left(-\frac{1}{a}\right)^n, \left(-\frac{3}{3a-1}\right)^n, \left(-\frac{3}{3a-1}\right)^n n \right\} \quad (\% \text{ o8})$$

(% i9) HypervanHoeij(RE[6],v[n],C);

Evaluation took 0.0160 seconds (0.0140 elapsed) using 3.561 MB

$$\left\{ \frac{\left(-\frac{1}{a+1}\right)^n}{(n-2)(n-1)n}, \frac{\left(-\frac{1}{a}\right)^n (n^2 - 2an - 3n + 2a^2 + 4a + 2)}{(n-2)(n-1)n} \right\} \quad (\% \text{ o9})$$

(% i10) HypervanHoeij(RE[7],v[n],C);

Evaluation took 0.0470 seconds (0.0520 elapsed) using 14.558 MB

$$\left\{ \left(-\frac{1}{a}\right)^n (n + 3a + 1) \right\} \quad (\% \text{ o10})$$

(% i11) HypervanHoeij(RE[8],v[n],C);

Evaluation took 0.0150 seconds (0.0110 elapsed) using 2.561 MB

$$\left\{ \left(-\frac{1}{a+1}\right)^n \right\} \quad (\% \text{ o11})$$

(% i12) HypervanHoeij(RE[9],v[n],C);

Evaluation took 0.0000 seconds (0.0120 elapsed) using 2.810 MB

$$\{ \} \quad (\% \text{ o12})$$

(% i13) HypervanHoeij(RE[10],v[n],C);

Evaluation took 0.0160 seconds (0.0180 elapsed) using 6.373 MB

$$\left\{ \left(-\frac{1}{a}\right)^n (n+1)(n+2)(n+3)(n+4), \left(-\frac{1}{a-1}\right)^n (n+1)(n+2)(n+3)(n+4)(n-a+6) \right\} \quad (\% \text{ o13})$$

(% i14) HypervanHoeij(RE[11],v[n],C);

Evaluation took 0.0000 seconds (0.0000 elapsed) using 0 bytes.

{ } (% o14)

(% i15) HypervanHoeij(RE[12],v[n],C);

Evaluation took 0.0310 seconds (0.0360 elapsed) using 12.809 MB

$\left\{ \frac{(-\%i)^n}{n!}, \frac{(-1)^{\frac{n}{2}}}{n!} \right\}$ (% o15)

(% i16) HypervanHoeij(RE[13],v[n],C);

Evaluation took 0.0160 seconds (0.0130 elapsed) using 3.623 MB

$\left\{ \frac{\left(-\frac{1}{a}\right)^n (n-3a-3)}{(n-3)(n-2)(n-1)n}, \frac{\left(-\frac{3}{3a+2}\right)^n (n+3a-1)}{(n-3)(n-2)(n-1)n} \right\}$ (% o16)

(% i17) HypervanHoeij(RE[14],v[n],C);

Evaluation took 0.0150 seconds (0.0050 elapsed) using 1023.766 KB

$\left\{ \left(-\frac{1}{a-1}\right)^n \right\}$ (% o17)

(% i18) HypervanHoeij(RE[15],v[n],C);

Evaluation took 0.9850 seconds (0.9840 elapsed) using 512.098 MB

$\left\{ \left(-\frac{1}{a-1}\right)^n, \left(-\frac{1}{a+1}\right)^n, \left(-\frac{a-\%i}{a^2+1}\right)^n, \left(-\frac{a+\%i}{a^2+1}\right)^n \right\}$ (% o18)

(% i19) HypervanHoeij(RE[16],v[n],C);

Evaluation took 0.0310 seconds (0.0370 elapsed) using 13.496 MB

{ } (% o19)

(% i20) HypervanHoeij(RE[17],v[n],C);

Evaluation took 0.0160 seconds (0.0130 elapsed) using 3.749 MB

{ } (% o20)

(% i21) HypervanHoeij(RE[18],v[n],C);

Evaluation took 0.0150 seconds (0.0200 elapsed) using 6.685 MB

{ } (% o21)

(% i22) HypervanHoeij(RE[19],v[n],C);

Evaluation took 0.0470 seconds (0.0470 elapsed) using 17.994 MB

$$\left\{ \left(-\frac{1}{a} \right)^n, \frac{\left(-\frac{1}{a} \right)^n}{(n-1)n} \right\} \quad (\% \text{ o22})$$

(% i23) HypervanHoeij(RE[20],v[n],C);

Evaluation took 0.0470 seconds (0.0470 elapsed) using 12.433 MB

$$\left\{ \frac{\left(-\frac{1}{a} \right)^n}{(n-4)(n-3)(n-2)(n-1)n} \right\} \quad (\% \text{ o23})$$

(% i24) HypervanHoeij(RE[21],v[n],C);

Evaluation took 0.0470 seconds (0.0540 elapsed) using 21.120 MB

$$\left\{ \left(-\frac{1}{a-1} \right)^n, \left(-\frac{1}{a} \right)^n, \left(-\frac{2}{2a+1} \right)^n, \left(-\frac{1}{a} \right)^n n \right\} \quad (\% \text{ o24})$$

(% i25) HypervanHoeij(RE[22],v[n],C);

Evaluation took 0.0150 seconds (0.0030 elapsed) using 831.703 KB

{ } (% o25)

(% i26) HypervanHoeij(RE[23],v[n],C);

Evaluation took 0.0320 seconds (0.0360 elapsed) using 12.809 MB

$$\left\{ \frac{(-\%i)^n}{n!}, \frac{(-1)^{\frac{n}{2}}}{n!} \right\} \quad (\% \text{ o26})$$

(% i27) HypervanHoeij(RE[24],v[n],C);

Evaluation took 0.0470 seconds (0.0460 elapsed) using 16.119 MB

$$\left\{ \frac{1}{n!}, \frac{(-1)^n}{n!} \right\} \quad (\% \text{ o27})$$

(% i28) HypervanHoeij(RE[25],v[n],C);

Evaluation took 0.0000 seconds (0.0050 elapsed) using 1.249 MB

{ } (% o28)

(% i29) HypervanHoeij(RE[26],v[n],C);

Evaluation took 0.1400 seconds (0.1440 elapsed) using 62.676 MB

$$\left\{ \frac{1}{n!}, \frac{(-\%i)^n}{n!}, \frac{\left(\frac{\sqrt{3}\%i-1}{2}\right)^n}{n!}, \frac{\left(-\frac{\sqrt{3}\%i+1}{2}\right)^n}{n!}, \frac{n}{n!}, \frac{(-1)^{\frac{n}{2}}}{n!}, \frac{(-1)^n}{n!} \right\} \quad (\% o29)$$

(% i30) HypervanHoeij(RE[27],v[n],C);

Evaluation took 2.7810 seconds (2.7870 elapsed) using 971.618 MB

$$\left\{ \left(-\frac{1}{a-1}\right)^n, \left(-\frac{1}{a+1}\right)^n \right\} \quad (\% o30)$$

(% i31) HypervanHoeij(RE[28],v[n],C);

Evaluation took 0.2500 seconds (0.2420 elapsed) using 108.566 MB

$$\left\{ \frac{(-\%i)^n}{n!}, \frac{(-1)^{\frac{n}{2}}}{n!} \right\} \quad (\% o31)$$

(% i32) HypervanHoeij(RE[29],v[n],C);

Evaluation took 5.2810 seconds (5.3110 elapsed) using 3643.480 MB

$$\left\{ \left(-\frac{1}{a-1}\right)^n, \left(-\frac{1}{a+1}\right)^n \right\} \quad (\% o32)$$

(% i33) HypervanHoeij(RE[30],v[n],C);

Evaluation took 0.4220 seconds (0.4240 elapsed) using 250.607 MB

$$\left\{ \left(-\frac{1}{a-1}\right)^n, \left(-\frac{1}{a+1}\right)^n, \frac{(-\%i)^n}{n!}, \frac{(-1)^{\frac{n}{2}}}{n!} \right\} \quad (\% o33)$$

(% i34) HypervanHoeij(RE[31],v[n],C);

Evaluation took 0.0000 seconds (0.0050 elapsed) using 703.859 KB

$$\left\{ \frac{(-\%i)^n}{n!}, \frac{(-1)^{\frac{n}{2}}}{n!} \right\} \quad (\% o34)$$

(% i35) HypervanHoeij(RE[32],v[n],C);

Evaluation took 0.0000 seconds (0.0080 elapsed) using 2.062 MB

$\{\}$ (% o35)

(% i36) HypervanHoeij(RE[33],v[n],C);

Evaluation took 0.0780 seconds (0.0850 elapsed) using 34.504 MB

$\left\{ \left(-\frac{1}{a-1} \right)^n, \left(-\frac{1}{a} \right)^n \right\}$ (% o36)

(% i37) HypervanHoeij(RE[34],v[n],C);

Evaluation took 0.0160 seconds (0.0110 elapsed) using 2.749 MB

$\left\{ \left(-\frac{1}{a+2} \right)^n (n+1) \right\}$ (% o37)

(% i38) HypervanHoeij(RE[35],v[n],C);

Evaluation took 0.0000 seconds (0.0040 elapsed) using 1.062 MB

$\{\}$ (% o38)

(% i39) HypervanHoeij(RE[36],v[n],C);

Evaluation took 0.0310 seconds (0.0260 elapsed) using 8.684 MB

$\left\{ \left(-\frac{1}{a-1} \right)^n \right\}$ (% o39)