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**Foupuagnigni, M. (CM-YND-MSD); Koepf, W. (D-KSSL-MI); Ronveaux, A. (B-NDP)****On factorization and solutions of  $q$ -difference equations satisfied by some classes of orthogonal polynomials. (English summary)***J. Difference Equ. Appl.* **10** (2004), no. 8, 729–747.[33D45 \(33C45 39A13\)](#)[Journal](#)[Article](#)[Doc Delivery](#)[References: 28](#)

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Summary: “We derive and factorize the fourth-order  $q$ -difference equations satisfied by orthogonal polynomials obtained from some perturbations of the recurrence coefficients of  $q$ -classical orthogonal polynomials. These perturbations include the  $r$ th associated, the anti-associated, the general co-recursive, co-recursive associated, co-dilated and the general co-modified  $q$ -classical orthogonal polynomials. Moreover, we find a basis of four linearly independent solutions of these fourth-order  $q$ -difference equations and express the modified families in terms of the starting ones.”

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Note: This list reflects references listed in the original paper as accurately as possible with no attempt to correct errors.

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